Graduate Operating Systems

Fall 2021

Paper “RM/EDF”

• The correctness of the system
  – Logical/functional
  – Temporal
• RT computing
  – The objective of “fast computing” is to minimize the average response time
  – The objective of real-time computing is to meet the individual timing requirement of each task
Paper “RM/EDF”

- Hard vs. soft real-time
- Closed-loop control

![Diagram of control system]

- Reference input $r(t)$
- A/D conversion
- Control-law computation
- D/A conversion
- Sensor
- Plant
- Actuator
- Outside effects
- The system being controlled

Paper “RM/EDF”

- Job
  - Each unit of work that is scheduled and executed by the system
- Task
  - A set of related jobs
  - For example, a periodic task $T_i$ consists of jobs $J_1, J_2, J_3, \ldots$ coming at every period
- Release time
  - Time instant at which a job becomes available for execution
  - It can be executed at any time at or after the release time
- Deadline
  - Time instant by which a job should be finished
  - Relative deadline: Maximum allowable response time
  - Absolute deadline = release time + relative deadline
Paper “RM/EDF”

- Periodic task $T_i$
  - Period $P_i$
  - Worst case execution time $C_i$
  - Relative deadline $D_i$

- Job $J_{ik}$
  - Absolute deadline = release time + relative deadline
  - Response time = finish time – release time

- Deadline miss if
  - Finish time > absolute deadline
  - Response time of $J_{ik}$ > $D_i$

Periodic Task Model

$Task = \{T, C, D\}$

jobs ($j_1, j_2, j_3, \ldots$)
Paper “RM/EDF”

- Table-driven scheduling
- Jitter
- Hyperperiods

A scheduling algorithm S is optimal if S cannot schedule a real-time task set T, no other scheduling algorithm can schedule T

- E.g., Rate Monotonic & EDF
Common Assumptions

- Single processor
- Every task is periodic
- Deadline = period
- Tasks are independent
- WCET of each task is known
- Zero context switch time

Paper “RM/EDF”

- Fixed priority system
  - Assign the same priority to all the jobs in each task
  - Rate monotonic (RMS)
- Dynamic priority system
  - Assign different priorities to the individual jobs in each task
  - Earliest Deadline First (EDF)
Paper “RM/EDF”

• RMS: optimal fixed priority scheduling algorithm

• Shorter period $\rightarrow$ Higher priority
  – Higher rate $\rightarrow$ higher priority

• Utilization bound

$$U = \sum_{i=1}^{n} C_i / T_i \leq n(\sqrt{2} - 1)$$

$$\lim_{n \to \infty} n(\sqrt{2} - 1) = \ln 2 \approx 0.693147 \ldots$$

RMS (Rate Monotonic Scheduling)

Process $P_1$: service time = 20, period = 50, deadline = 50
Process $P_2$: service time = 35, period = 100, deadline = 100
Missed Deadlines with RMS

Process $P_1$: service time = 25, period = 50, deadline = 50
Process $P_2$: service time = 35, period = 80, deadline = 80

RMS is guaranteed to work if

$$N = \text{number of processes}$$

$$u = \sum_{i=1}^{N} \frac{f_i}{P_i} \leq N \left( \sqrt{2} - 1 \right);$$

$$\lim_{N \to \infty} N \left( \sqrt{2} - 1 \right) = \ln 2 \approx 0.693147$$

<table>
<thead>
<tr>
<th>$N$</th>
<th>$N \left( \sqrt{2} - 1 \right)$</th>
</tr>
</thead>
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<tr>
<td>2</td>
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<tr>
<td>20</td>
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</tbody>
</table>

Paper “RM/EDF”

- EDF: shorter absolute deadline $\rightarrow$ Higher priority
- Utilization bound $U_b = 1$
- $U_b$ is necessary and sufficient
EDF (Earliest Deadline First)

Process $P_1$: service time = 25, period = 50, deadline = 50
Process $P_2$: service time = 35, period = 80, deadline = 80

Paper “RM/EDF”

- RMS
  - RMS may not guarantee schedulability even when $U < 1$
  - Low overhead: priorities do not change for a fixed task set

- EDF
  - EDF guarantee schedulability as long as $U \leq 1$
  - High overhead: task priorities may change dynamically
Paper “RM/EDF”

• Implementation complexity
  – Modifying systems vs. from scratch
  – Periods for newly arriving tasks
  – Fixed vs. infinite number of priority levels
  – EDF runtime overheads (priorities change)

  – Winner: RMS

Paper “RM/EDF”

• Run-time overhead
  – Updating deadlines costly
  – EDF: fewer context switches (preemptions)

*Figure 1. Preemptions introduced by RM (a) and EDF (b) on a set of two periodic tasks. Adjacent jobs of $\tau_i$ are depicted with different colours to better distinguish them.*
Paper “RM/EDF”

• Run-time overhead

![Graph 1](image1)

![Graph 2](image2)

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Paper “RM/EDF”

• Run-time overhead

![Graph 3](image3)

• Winner: EDF
Paper “RM/EDF”

• Schedulability analysis
  – EDF (d=p): simple
  – RMS: U <= 0.69; simple, but resources wasted
    • Hyperbolic bound (higher acceptance ratio for large n)
  – Exact for EDF:
    • Processor Demand Criterion (PDC) for d<p
  – Exact for RMS:
    • Response Time Analysis (RTA)

• Winner: Tie?
Paper “RM/EDF”

- Robustness during overloads
  - Permanent
    - Winner: RMS

- Robustness during overloads
  - Transient
    - Winner: Tie
Paper “RM/EDF”

• Jitter and Latency

• Winner: Tie?

Paper “RM/EDF”

• Resource sharing
  – Solutions for EDF and RMS exist

• Aperiodic tasks
  – Periodic servers (EDF has higher utilization bounds)

• Resource reservations
  – Reservation protocols exist for EDF and RMS