

Graduate Operating Systems

Spring 2022

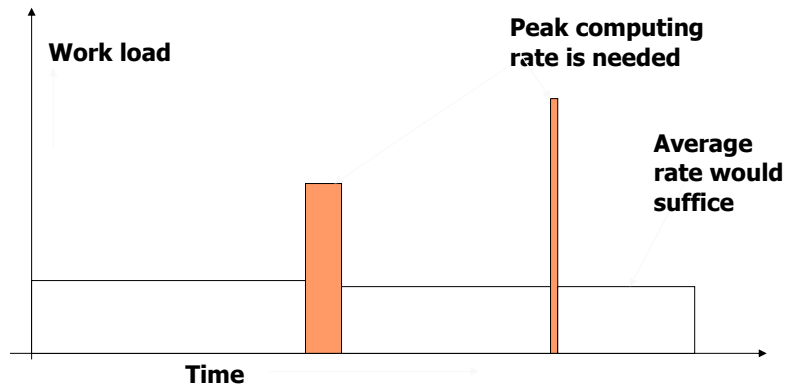
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Paper “DVS”

- Real-Time Systems
- Dynamic Voltage Scaling (DVS, DFS)
- Over-designed systems (peak performance)
- Periodic task model
- Earliest Deadline First (EDF)
- Rate Monotonic Scheduling (RM)
- Schedulability test

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Peak vs. Average Performance

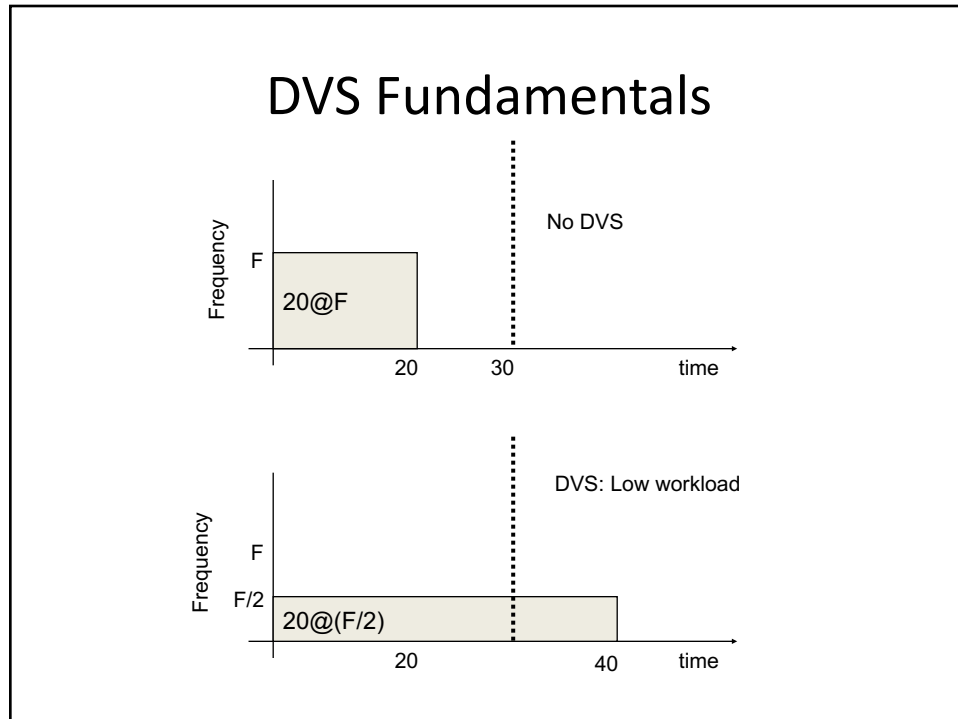


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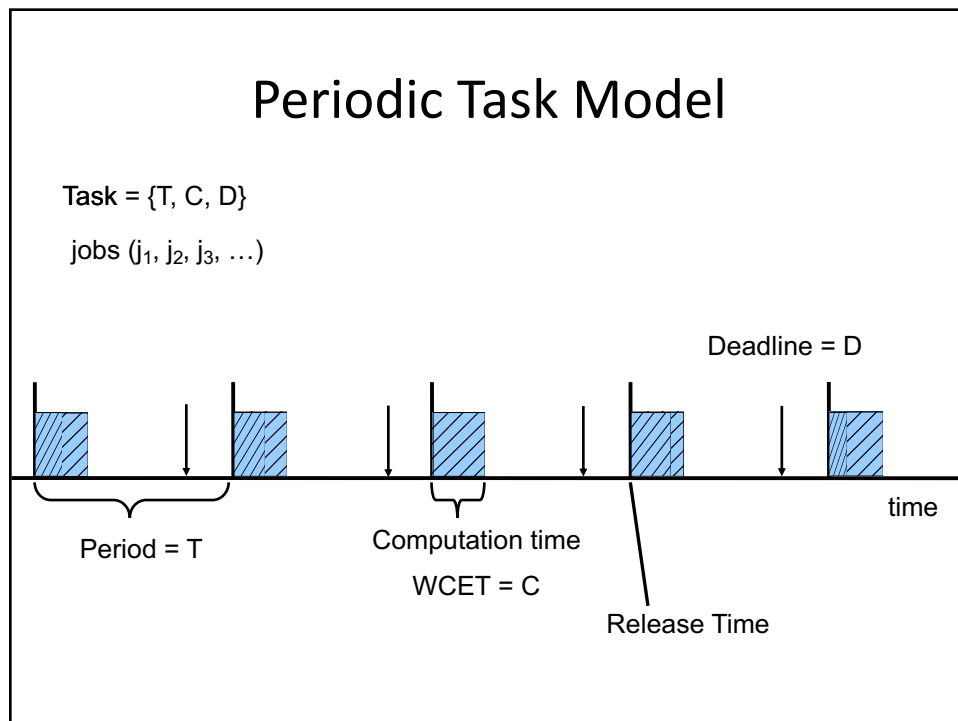
DVS Fundamentals

- Processors are based on CMOS technology where dynamic power is the bottleneck
- Dynamic power (due to switching activity)
 - Power depends on V^2 and f
 - Achievable f depends on V
- Energy = $P * t_{\text{execution}}$

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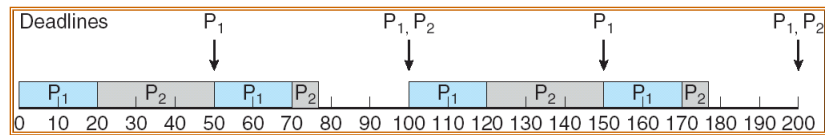


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RMS (Rate Monotonic Scheduling)

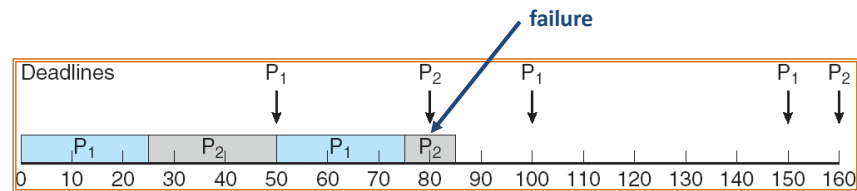
Process P₁: service time = 20, period = 50, deadline = 50

Process P₂: service time = 35, period = 100, deadline = 100



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Missed Deadlines with RMS



Process P₁: service time = 25, period = 50, deadline = 50

Process P₂: service time = 35, period = 80, deadline = 80

RMS is guaranteed to work if

N = number of processes
sufficient condition

$$u = \sum_{i=1}^N \frac{t_i}{p_i} \leq N(\sqrt[N]{2} - 1);$$

$$\lim_{N \rightarrow \infty} N(\sqrt[N]{2} - 1) = \ln 2 \approx 0.693147$$

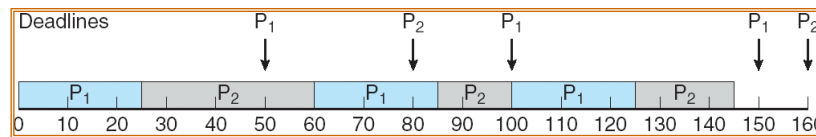
N	$N(\sqrt[N]{2} - 1)$
2	0,828427
3	0,779763
4	0,756828
5	0,743491
10	0,717734
20	0,705298

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EDF (Earliest Deadline First)

Process P₁: service time = 25, period = 50, deadline = 50

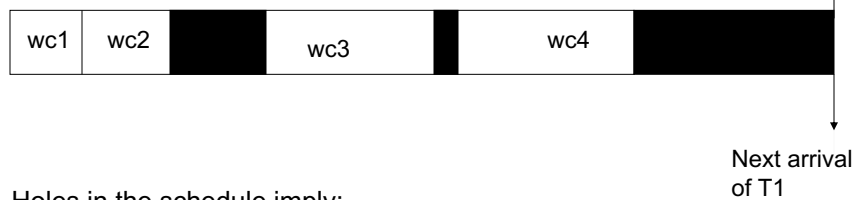
Process P₂: service time = 35, period = 80, deadline = 80



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Static Voltage Scaling EDF: Motivation

WC_i = worst case computation time @ F_{max}



Holes in the schedule imply:

EDF Test: $\sum(wc_i/p_i) < 1$ at frequency = F_{max}

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Static Voltage Scaling EDF

EDF Test:
 $\sum(wc_i/p_i) < 1$ at maximum frequency = F_{max}

Static-VS EDF Test:
 $K * [\sum(wc_i/p_i)] = 1$ at frequency = F_{max}/K

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Static EDF: Example

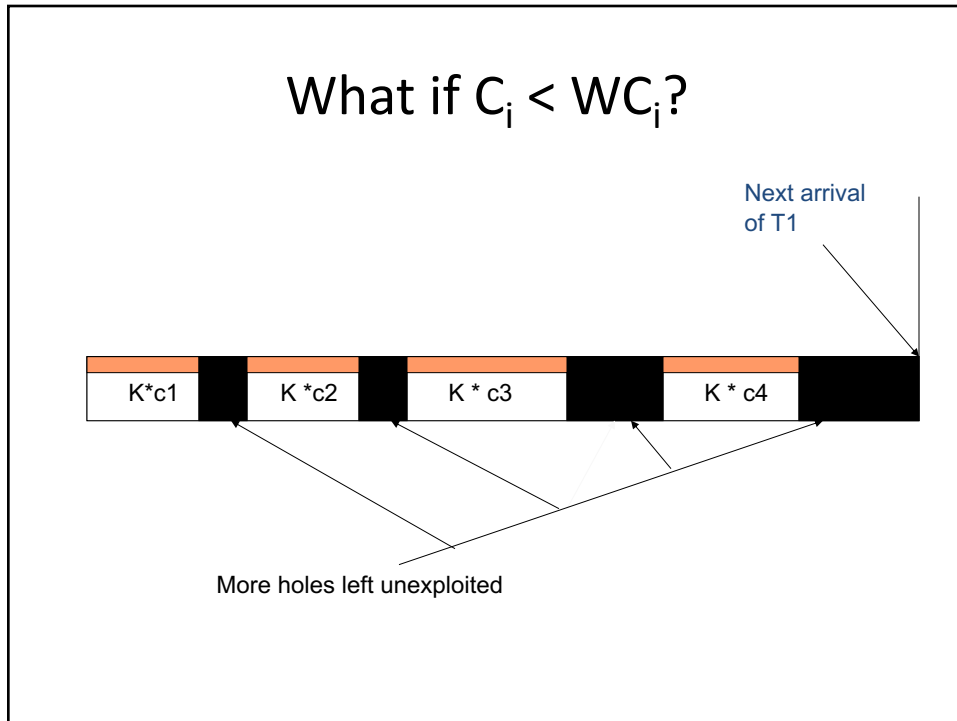
Task	Computing Time	Period
1	3 ms	8 ms
2	3 ms	10 ms
3	1 ms	14 ms

Available frequencies:
1.00, 0.75

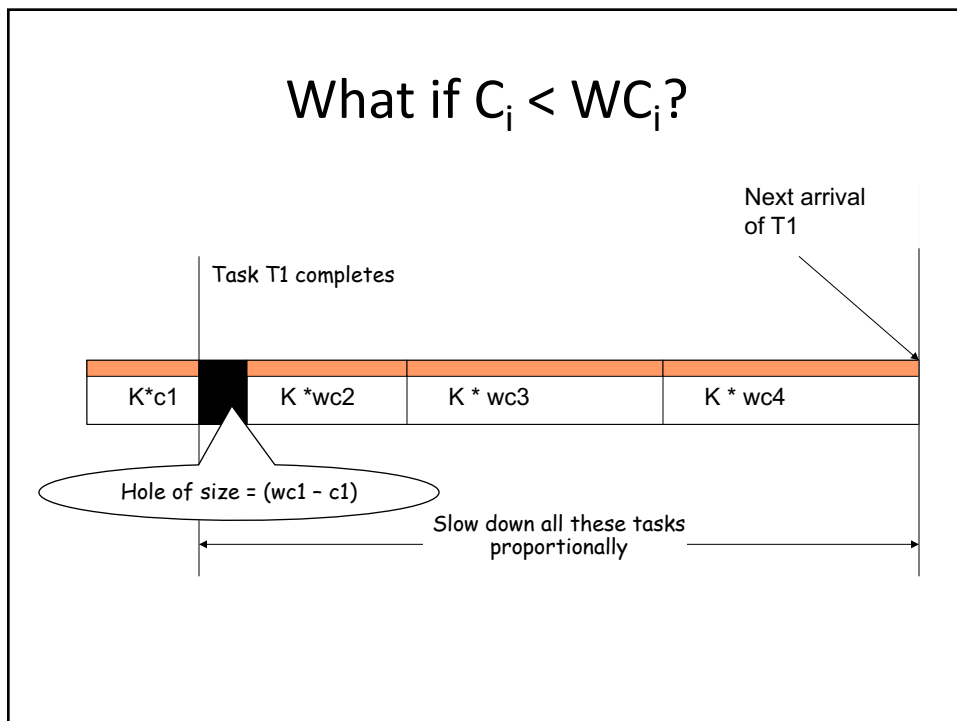
Schedulability test for $\alpha = 1.00$
 $3/8 + 3/10 + 1/14 \leq 1 \rightarrow$ **Return true**

Schedulability test for $\alpha = 0.75$
 $3/8 + 3/10 + 1/14 \leq 0.75 \rightarrow$ **Return true**

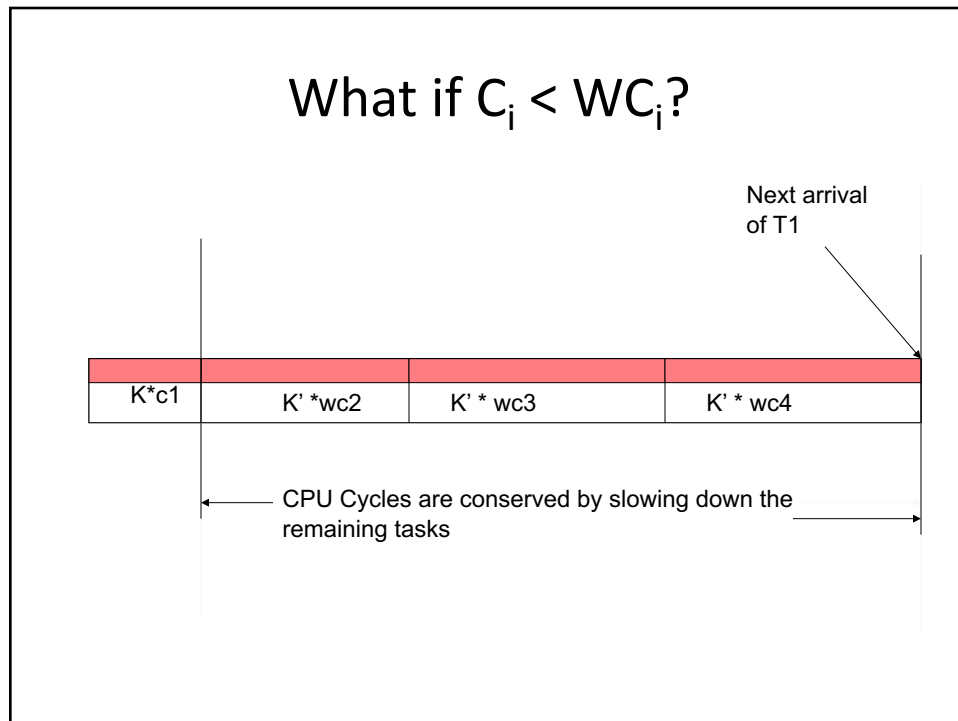
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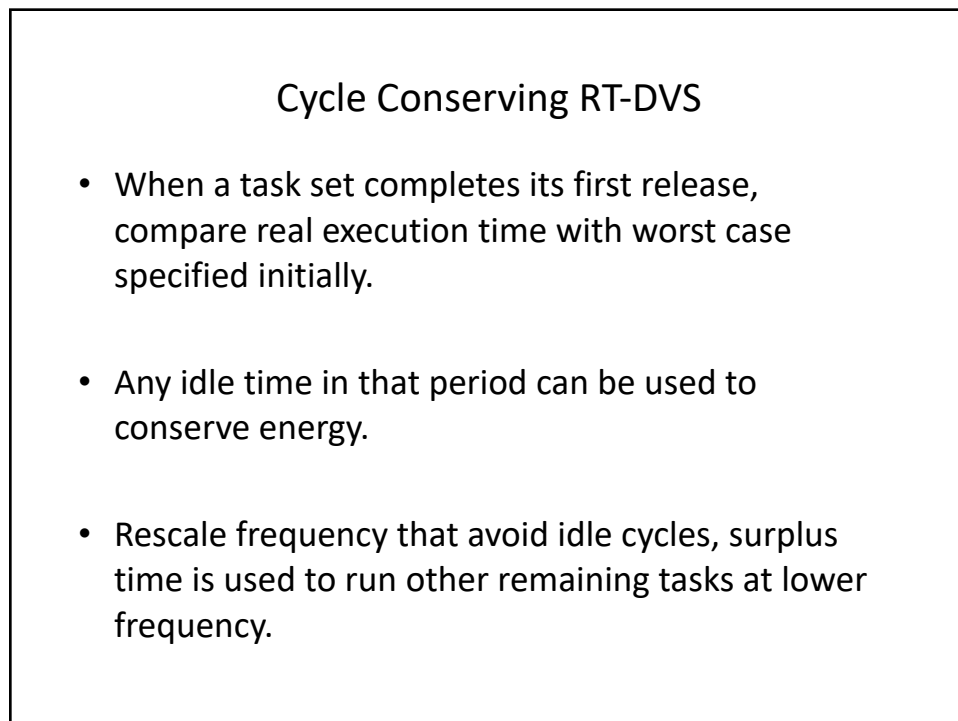
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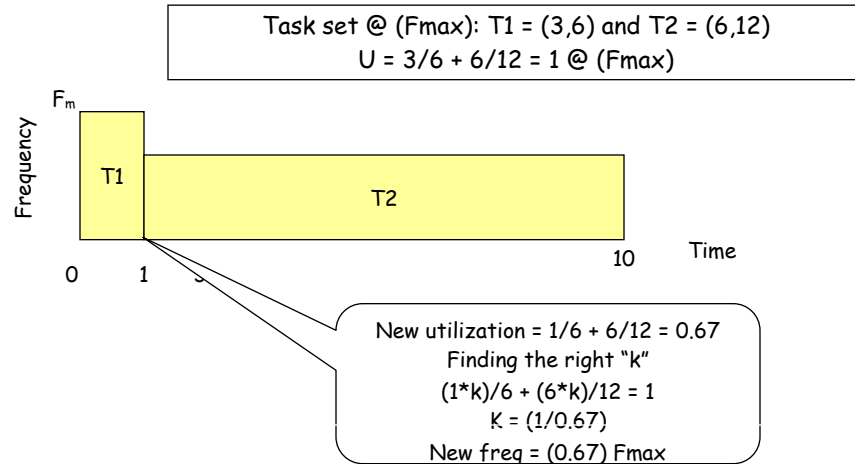


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Cycle Conserving EDF: Example

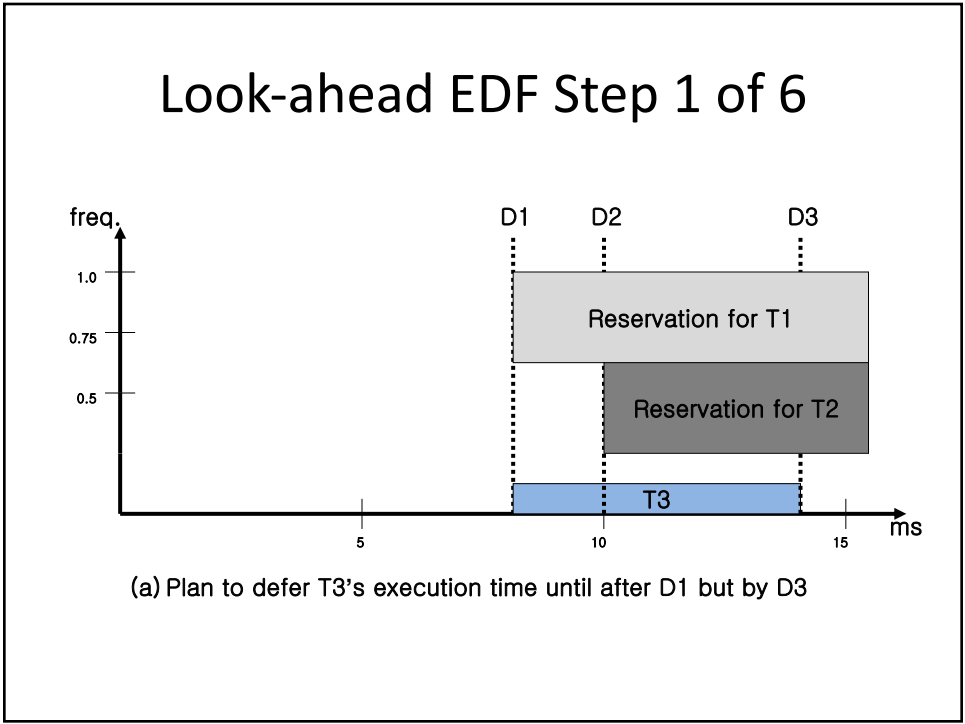


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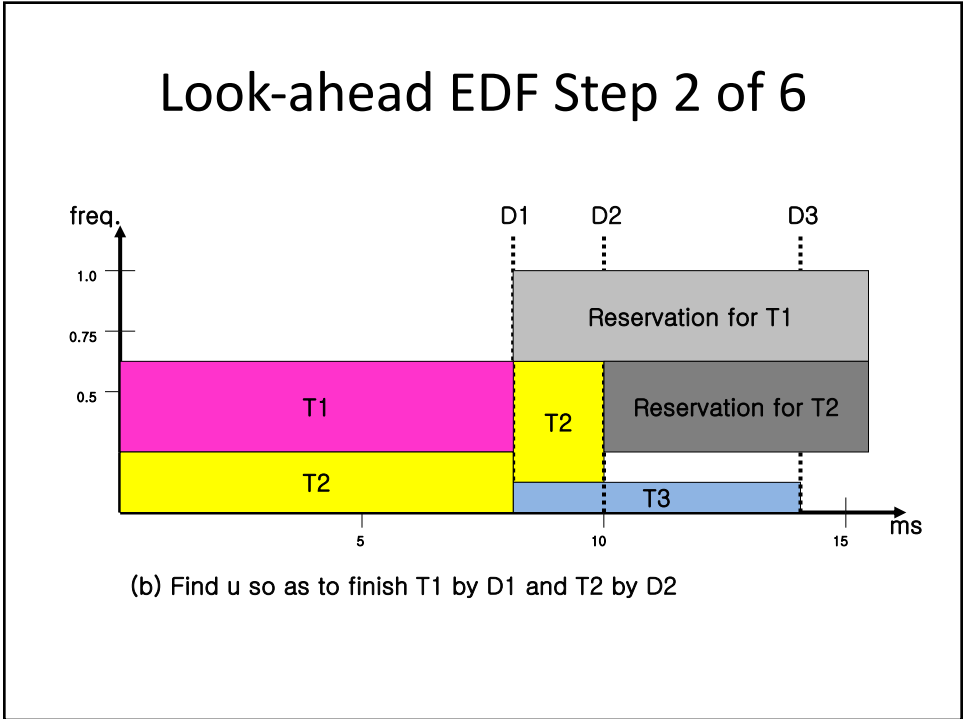
Look-Ahead EDF

- Defer as much work as possible and set initially to the minimum possible frequency.
- Hence at later stage if a task uses much less than its worst case, deferred work may never be needed.
- It ensures that there are sufficient cycles available for each task to meet its deadline after reserving cycles for higher priority jobs.
- Best saving of energy.

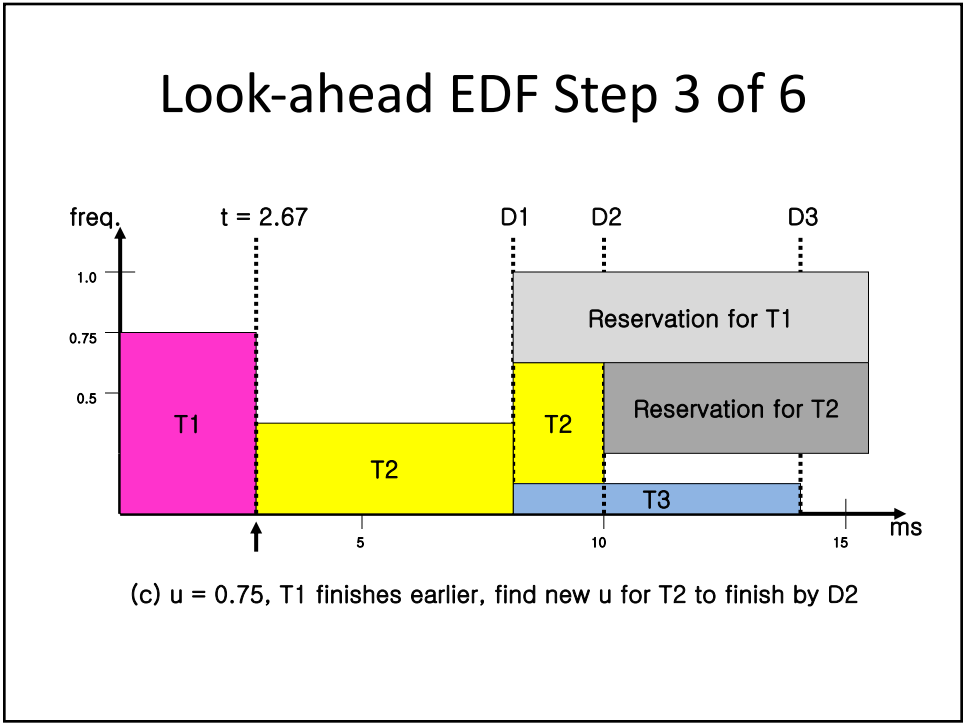
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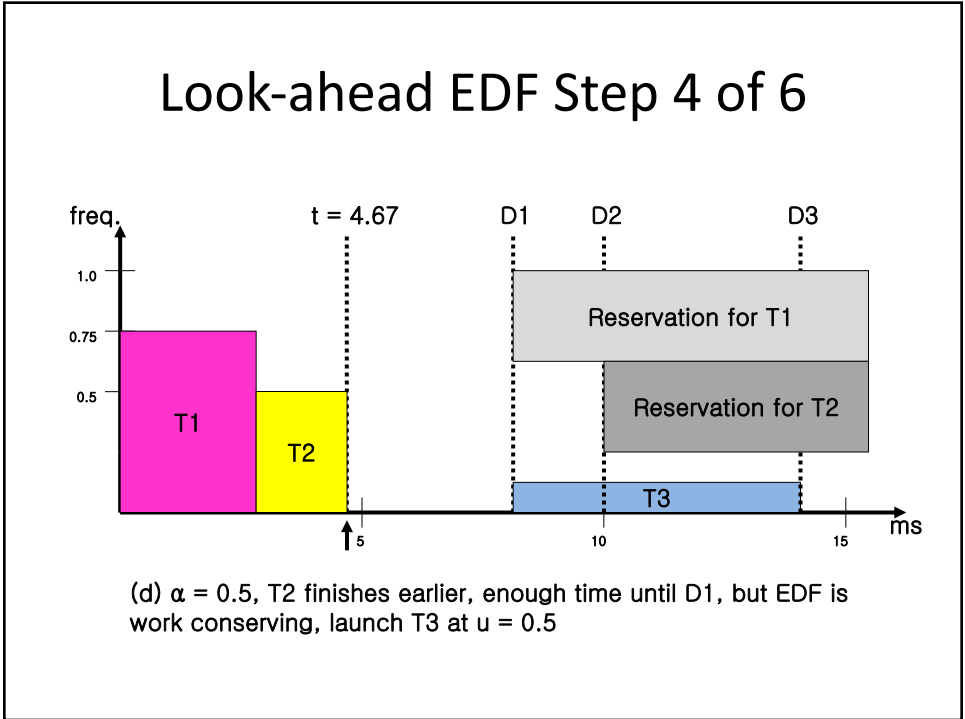
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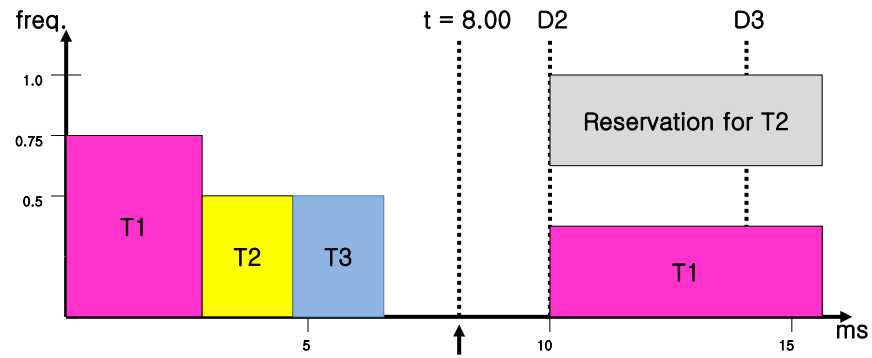


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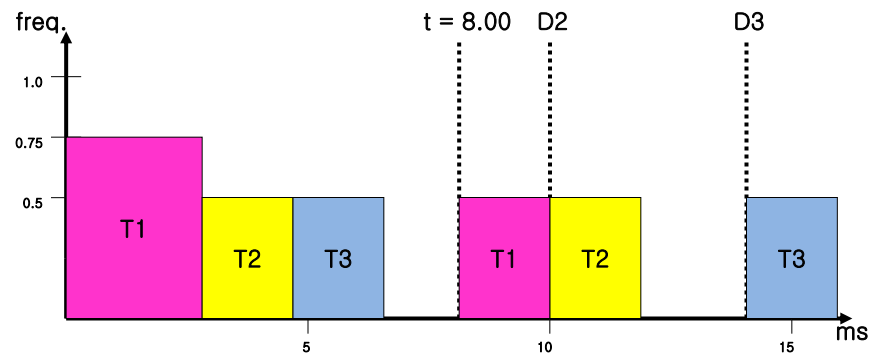
Look-ahead EDF Step 5 of 6



(e) Guess for T1 again

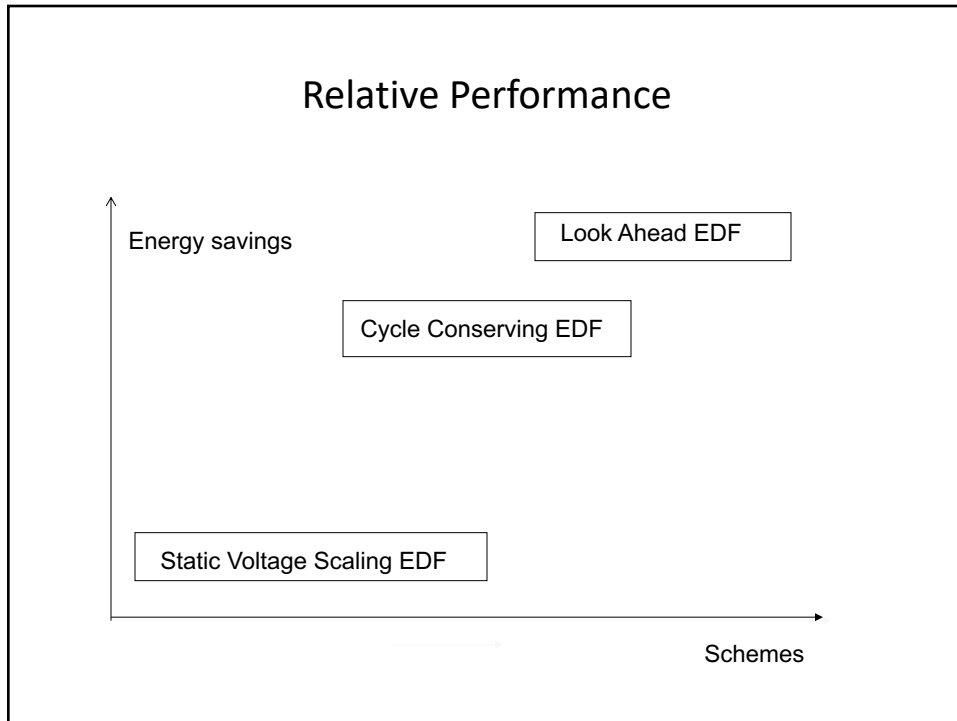
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Look-ahead EDF Step 6 of 6



(f) $u = 0.5$, every task is dynamically scheduled successfully

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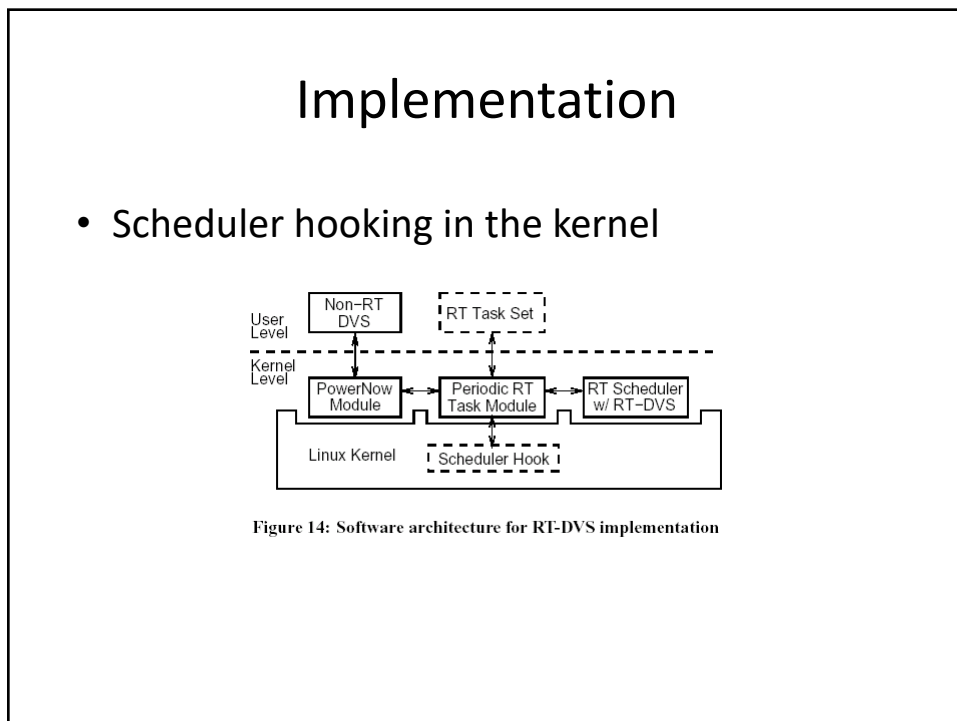


Figure 14: Software architecture for RT-DVS implementation

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